

British Informatics Olympiad Final

6–8 April, 2001

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Code Book

Alpha complex is large and sprawling, its many rooms and corridors designed to confuse the uninitiated. Its filing system is even worse. Several years ago they moved over to a new digital “it is not analogue, so it must be good” system. Every word that is used in filing reports has been encoded by a unique binary number, so reports just consist of long sequences of 0s and 1s. The system has three saving graces:

- The encoding is unambiguous; i.e. no encoded word is the prefix of another encoded word. For example, if 010 is a word there can be no other words beginning with 010 and the words 0 and 01 will not exist.
- The lexicographic order of the words has been maintained. In other words, if $word_1$ is before $word_2$ in the dictionary, the encoding of $word_1$ would also be before the encoding of $word_2$. (In the lexicographic ordering of numbers they are aligned on the left, so 10001 is before 101 but after 100.)
- The encoding is optimal. If you counted how many 0s and 1s are used in total over all the words in all the files, it would not be possible to lower this number by using a different encoding that obeys the previous two rules.

For example, if there were three words that were encoded, the first (lexigraphically) occurring 5 times, the second 8 and the third 6 the encoding would be 00, 01 and 1. This has an overall total of $5 \times 2 + 8 \times 2 + 6 = 32$. Another encoding that meets the first two conditions would be 0, 10 and 11, but this has a score of 33 so does not meet the final condition. The encoding 00, 1 and 01, which would have a score of 30, does not meet the second condition. The encoding 10, 0 and 1 (with a score of 24) does not meet the first condition since 10 is ambiguous (is it 10 or 1 then 0?)

Write a program that, given a list of word frequencies (corresponding to words in lexicographic order) calculates an encoding that meets all three conditions. The first line of input will consist of a single integer, n ($1 \leq n \leq 100$), indicating the number of frequencies to follow. The next n lines will each consist of a single number (between 1 and 100 inclusive), the i^{th} line indicating the frequency of the i^{th} word in lexicographic order.

You should output n lines. The i^{th} line should consist of your encoding for the i^{th} word.

Sample Input

```
3
5
8
6
```

Sample Output

```
00
01
1
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